Sharing architecture knowledge through models: quality and cost

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Abstract

In the field of software architecture, there has been a paradigm shift from describing structural information, such as components and connectors, to documenting Architectural Knowledge (AK), such as design decisions and rationale. To this end, a series of industrial and academic domain models have been proposed for defining the concepts and their relationships in the field of AK. To a large extent the merit of this new paradigm is to share and reuse AK across organizations, especially in geographically distributed settings. However, the employment of different AK domain models by different parties makes effective AK sharing challenging, as it needs to be mapped from one domain model to another. In this paper, we investigate two different approaches for sharing AK, based on either direct or indirect mapping between different AK domain models. We compare the cost and quality of these two approaches, with respect to the processing of large amounts of AK instances. To predict the quality and costs of this processing in advance, a prediction model is proposed and validated with a concrete AK sharing case. Based on the comparison results, stakeholders involved with AK sharing can select an appropriate approach by trading off quality and cost in their own context.

1 Introduction

Software architecture is considered of paramount importance to the software development life cycle (Bass et al., 2003). It is a key artifact for the early analysis of the system, as it facilitates stakeholders communication and understanding, and drives both system construction and evolution. Current research trends in software architecture focus on the treatment of architectural decisions (Kruchten, 2004; Kruchten et al., 2005; Tyree & Akerman, 2005) as first-class entities (Bosch, 2004) with explicit representation in the architectural documentation (Jansen & Bosch, 2005). Kruchten et al. (2005) define architecture knowledge (AK) as: $AK = \text{design decisions} + \text{design}$, in which four types of design decisions are classified. Generally speaking, AK encompasses not only decisions and rationale, but also other architecturally-significant information. For example, the AK core model proposed by de Boer et al. (2007) suggests that AK is a set of relationships between decisions, stakeholders, architectural design, and processes. AK may contain alternative solutions, significant entities from the problem space (e.g. key stakeholder concerns), technology constraints, business information, general knowledge (e.g. design patterns) etc. (Avgeriou et al., 2007).

The main value of a software company is its intellectual capital and AK is deemed a valuable part of this (Kruchten et al., 2005). It is in the interest of companies to share AK, e.g. by recording the knowledge from the architects’ minds on paper, or further formalizing it in a knowledge repository, so that individual expertise and collective decisions on AK can be shared
among stakeholders. Although sharing and reusing of AK is far from common practice at present (Tang et al., 2006), it is considered as a dominant factor in a software architecting process and for eventual project success (Jansen & Bosch, 2005). AK sharing may serve significant architecting activities like modifying past design decisions, or performing architecture reviews and trading off quality attribute requirements. It may also play a simpler role, e.g. in a cross-team software development project, all the stakeholders must have access to information on who is responsible for which part of the whole system.

Sharing AK between different organizations, or even between the departments of a single organization, poses a great challenge: the domain models of AK are not standardized. On the contrary, they tend to vary enormously. In fact, various authors (Kruchten, 2004; Tyree & Akerman, 2005; Tang et al., 2007; Capilla et al., 2006; Ali-Babar et al., 2006, Jansen et al., 2008) have proposed their own AK domain models to document AK concepts and their relationships. Some of these concepts and relationships are different, while others are largely overlapping. These discrepancies between the AK domain models can hamper the effective sharing of AK, which in turn results in misunderstandings among stakeholders, expensive system evolution, and limited reusability of architectural artifacts (Jansen et al., 2007). This problem is of course not specific in the field of AK but it is very common in other fields, such as knowledge sharing in gene data (Camon et al., 2004) and geographic information systems (Fonseca et al., 2000) etc.

In this paper, we look at the problem of AK sharing through a knowledge grid (Zhuge, 2004; Jansen et al., 2007). In this envisioned AK grid, AK is captured in domain-specific models. The use of such models allows different organizations, departments, or even persons to express their AK using their own concepts in the AK grid. Using the mappings between these models, all AK is transparently shared among the interested stakeholders, as the AK is expressed for each person in terms of his or her own domain model(s). Two different approaches for implementing this AK sharing strategy are investigated in this paper. The first approach is a direct mapping approach, in which all models are directly mapped onto each other. The second approach is an indirect mapping approach, in which all the models map onto one central model. This central model acts a mediator between the different domain models. The topic of this paper is to find out the quality of both AK sharing approaches and the cost associated with them.

Both the cost and the quality of AK sharing is not only dependant on the models and mappings involved, but also on the actual AK instances of these models. Only with these instances the real cost and quality of AK sharing can be determined. However, creating these instances entails considerable effort, as human intervention is required. To make matters worse, most of this effort needs to continuously evolve when, due to further insight, domain models or mappings are changed. Hence, we would like to predict the cost and quality of AK sharing in advance before effort is spent on creating instances. This paper contributes such a prediction model for both the direct and indirect mapping approaches.

The rest of this paper is organized as follows. In section 2, we present related work about software architecture, AK, and knowledge sharing methods. The problem statement of evaluating AK sharing approaches with respect to cost and quality is refined in section 3. In section 4, a cost model for AK sharing is presented. Section 5 proposes three models for predicting the AK sharing quality. A concrete AK instance mapping experiment is presented in section 6 to validate these prediction models. A comparison is made on the difference in quality and cost between the two approaches for sharing AK in section 7. We wrap up with conclusions and future work in section 8.

2 Related work

2.1 Software architecture

In the early 1990s, Perry & Wolf (1992) formed the starting point for an evolving community that actively studied the notion and practical application of software architecture. In the years to follow, software architecture has been broadly adopted in the industry as well as in the
software engineering research community. A generally accepted definition of the notion of software architecture is captured in the IEEE 1471-2000 standard (IEEE, 2000): "software architecture is the fundamental organization of a system embodied in its components, their relationships to each other and to the environment and the principles guiding its design and evolution". This definition places component and their connectors, as the central concepts of software architecture. Architectural Description Languages (ADLs) (Medvidovic & Taylor, 2000) use these concepts as first-class entities to formally describe software architectures.

2.2 AK and AK sharing

The traditional approach of components and connectors has failed to address one of the major shortcomings in the field of software architecture: Architectural Knowledge Vaporization (Bosch, 2004; van der Ven et al., 2006), i.e. the architecturally significant information being lost during system evolution. To this end, Jansen & Bosch (2005) suggested to treat software architecture as a result of a set of architectural design decisions, which is one of the most significant forms of AK (Kruchten et al., 2005; van der Ven et al., 2006). The SHARK series of workshops (Lago & Avgeriou, 2006; Avgeriou et al., 2007) demonstrate the academic and industrial interests and advancement in AK sharing and reusing.

Various specific AK domain models have been proposed by industrial organizations (see the LOFAR AK model (Jansen et al., 2008) from the LOFAR project) and domain experts (see Kruchten’s ontology (Kruchten, 2004), Tyree’s template (Tyree & Akerman, 2005), AREL (Tang et al., 2007), PAKME (Ali-Babar et al., 2006), ADDSS (Capilla et al., 2006) and Archium (Jansen et al., 2007) AK models). There are also generic AK models, such as the IEEE 1471-2000 standard (IEEE, 2000), which define a domain model for architecture concepts that can be used for AK management. All these AK models are composed of a set of concepts and relationships between the concepts, and therefore ontologies can be used to model these AK models (Akerman & Tyree, 2005).

Preliminary work on investigating AK sharing in a knowledge grid has been performed by de Boer et al. (2007). They investigate the issues of AK sharing using an indirect mapping approach. To this end they construct a core model that covers most of the concepts from different AK domain models. The core model acts as a mediator for mapping between different AK models. Their work mainly focuses on a model and a conceptual level sharing solution which uses concept (i.e. model element) mappings. However, the issue of evaluating this core model with respect to AK sharing quality and cost has not been addressed. We extend this work, by looking in detail, into the quality and cost that such an approach brings.

2.3 Knowledge sharing approaches and tools

Wikis are an emerging web-based tool for cooperative knowledge management and sharing. The most famous and successful example of a wiki is Wikipedia. Wikis are very popular in cases that demand effective collaboration and knowledge sharing at low costs. Some concrete research effort has been made recently on using wiki for documentation of software requirements (Silveira et al., 2005), software architecture (Bachmann & Merson, 2005), software artifacts (Aguiar & David, 2005), and software development processes (Louridas, 2006). The limitation of a wiki is that it shares knowledge based on common topics (e.g. tags). A wiki therefore suffers from the same problem as AK sharing through models, as it requires stakeholders to share a common understanding and adopt common terminology. In addition, a wiki allows users to make different explanations for one topic, which may confuse the stakeholders who want to share the knowledge.

1LOFAR is the abbreviation of Low Frequency Array project undertaken by Astron, the Dutch Astronomy Institute, which is involved in the development of large software-intensive systems used for astronomy research.
Ontology is a key technology for knowledge representation, management and sharing, and has been widely used in some emerging fields, such as the semantic web. In the knowledge engineering domain, an ontology can be regarded as a conceptual model. This is confirmed by the commonly accepted definition in (Gruber, 1993): "An ontology is a specification of a conceptualization". In the emergent semantic web, search, interpretation and aggregation can be addressed by ontology-based semantic annotation (Uren et al., 2006), which can also be applied in document annotation for structuring, interpreting and sharing documents. This approach has standard annotation formats (e.g. RDF, OWL) as a prerequisite for sharing annotations, thus facilitating knowledge sharing and collaboration. The limitation of this approach is that all stakeholders involved with the knowledge sharing should agree on the ontology being used for the semantic annotation. This is desirable but highly unlikely to occur in practice.

Due to the existence of multiple ontologies in one application domain, there needs to be a reconciliation of heterogeneous ontologies for effective knowledge sharing. Ontology mapping is an activity to relate semantically two ontologies e.g. \( O_1 \) and \( O_2 \). Mapping one ontology onto another means that for each concept \( C \) in ontology \( O_1 \), we try to find a corresponding concept, which has the same intended meaning, in ontology \( O_2 \) (Ehrig & Staab, 2004). Many research efforts on ontology mapping methods (automatic or semi-automatic) have been taken to achieve good mapping result with less cost (Kalfoglou & Schorlemmer, 2003; Choi et al., 2006). However ontology mapping still remains an expensive, time-consuming and error-prone activity.

2.4 Ontology mapping quality and cost evaluation

As mentioned in section 2.3, ontology mapping is a promising approach for information exchange in a semantically sound manner (Kalfoglou & Schorlemmer, 2003), in which the meaning of information is taken into account. Ehrig & Euzenat (2005) have performed research on the evaluation of ontology mapping by introducing two criteria: the precision and recall rate. These metrics originate from information retrieval (IR) theory, and are revised as relaxed precision and recall rate, which is more appropriate for ontology mapping evaluation. The criteria are relaxed in the sense that they are not as strict as those for IR. The reason is that a mapping between similar ontologies is better in relevant data retrieval than a mapping between totally different ontologies, but these two cases are both regarded as the non-relevant data in IR. Euzenat (2007) extends this work by proposing semantic measures in order to get maximal precision and recall for correct ontology mappings. However, this work is limited in evaluating the quality of the mappings between ontologies in the conceptual level. For the ontology mapping cost, Ehrig & Staab (2004) proposed a cost-effective way QOM (Quick Ontology Mapping) for ontology mapping by introducing a restricted range of costly features, but they provide no quantified cost analysis for this mapping method. To the best of our knowledge, there is no research work on the quality and cost of instance mapping for knowledge sharing.

3 Analysis

3.1 Introduction

As mentioned in section 1, the research focus of this paper is on the prediction of AK sharing quality and cost. For AK sharing, two approaches can be employed: direct and indirect mapping. Section 3.2 presents how AK can be shared using concept mappings. Section 3.3 outlines how the cost of AK sharing is evaluated, whereas section 3.4 does this for quality.

3.2 Sharing AK using concept mappings

For the purpose of clarity, we generalize AK sharing in two levels: the conceptual level and the instance level. At the conceptual level, an AK model defines the concepts and relationships that a particular organization, department, project, or person uses. At the instance level, the instances of the aforementioned concepts and relationships exist. The sharing of AK instances based on
different AK models depends on the mutual understanding of the underlying AK models, i.e. one concept in one AK model can be translated or mapped into a concept in the other model. Thus this mutual understanding can be specified by a set of mapping relationships between concepts from different AK models.

For example, domain experts can define a concept $A$ in one AK model to have the same meaning as a concept $B$ in another AK model. Once the equality mapping relationship is defined between concepts $A$ and $B$, the instances (e.g. pieces of text) of concept $A$ are considered also to be instances of concept $B$.

To achieve AK sharing, we use the mappings defined between concepts of different AK models to translate the instances of one model into another. For the required model mappings, two approaches can be employed: a direct or an indirect mapping approach. With the direct mapping approach, one defines mapping relationships from a source AK model to a target AK model directly. The source AK model is the model in which the instances to be translated are defined. The target AK model is the language in which one would like to use the AK. An indirect mapping approach defines mapping relationships from a source AK model to a target AK model through a central model, which acts as a mediator.

Both methods have their pros and cons. In most cases, a direct mapping approach achieves a better AK sharing quality than the indirect one, as every translation is bound to lose some information. On the other hand, a direct mapping approach requires more effort to realize the mappings and is harder to maintain than an indirect mapping approach: with the direct approach, the number of mapping relationships increases exponentially with the number of AK models involved, whereas with the indirect approach the number of mapping relationships increases linearly. In other words, there is a tradeoff between the cost and the quality of the AK sharing when using these two approaches.

3.3 Evaluating the cost of sharing AK using model mappings

The cost of sharing AK using model mappings has many aspects. In this paper, we concentrate on those costs that come from human effort, thereby leaving out hardware and software costs. The cost for sharing AK using model mappings consists of the following different aspects:

- **Modeling costs.** Effort is needed to find the concepts and relationships that are relevant to AK and express them in AK models.
- **Capturing costs.** The aforementioned AK models need to be filled in with relevant data (AK instances), which is the most costly operation of all.
- **Mapping costs.** To share AK, mapping definitions among the AK models are needed.
- **Evolution costs.** Further insights into a domain can cause changes to the used AK models.
- **Extension costs.** An organization, department or person might want to join the knowledge grid and extend it with their own AK model.

The challenge is to find ways to quantify these aspects of the cost. Such quantifications do not have to provide absolute numbers, as relative numbers or even the order magnitude of these numbers is useful enough in making coarse-grained comparisons between different approaches.

3.4 Evaluating the quality of sharing AK using model mappings

3.4.1 Query-based AK-sharing scenario

We envision AK sharing in an AK grid, i.e. a heterogeneous AK repository, that is comprised of different local repositories. Each local repository contains one AK model and its instances. A user can retrieve AK from all involved AK repositories transparently without being conscious of the underlying model differences. To quantify the quality, we use a specific user scenario in the form of a query, which is a typical activity for knowledge sharing. The query is a precise request...
for information retrieval, typically expressed as keywords combined with boolean operators and other modifiers.

The query-based scenario is shown in Figure 1. A user who understands only AK model $T$ queries the repository of AK model $S$ using concepts from AK model $T$ as query keywords. The conceptual difference between AK model $S$ and $T$ poses a problem for AK sharing. The concepts from model $T$ queried do not exist (or exist, but have a different meaning) in model $S$. Thus, the repository of model $S$ cannot return any data (AK instances). Using concept mappings from model $S$ to $T$, the repository of model $S$ could return partial data to the user.

![Figure 1 Query-based scenario for AK sharing](image)

**3.4.2 Model mappings**

To construct AK models, we use ontologies (see section 2.3). In ontologies, concepts are defined as classes. The mapping relationships between the concepts of the AK models are therefore defined as relationships between classes in an ontology. We use the following mapping relationships to relate AK models with each other:

- **subClassOf**, denotes one concept to be a specialization of another.
- **superClassOf**, denotes one concept to be a generalization of another.
- **equivalentClass**, denotes two concepts to be the same.
- **disjointWith**, denotes that the instances of two concepts can never belong to both concepts.
- **noMatchingPair**, denotes that a concept cannot be mapped to another AK model.

**3.4.3 Problematic mapping scenarios**

Both mapping approaches suffer from two problematic mapping scenarios that result in lost data and garbage data. Hence, these scenarios influence the mapping quality in a negative way. **Lost data** are created when the instances cannot be classified to the target model, as either the necessary concepts are missing in the target model or the defined concept mapping is incomplete. Consequently, queries are able to return less relevant data, hence data is lost. **Garbage data** are the instances that are wrongfully classified, thereby contaminating the relevant data in the query results. The instances can be wrongfully classified due to the following reasons:

- **Instance classification problems**, which sometimes occur with the **superClassOf** mapping relationship. If a concept is mapped as a **superClassOf** a concept in a target model, some of the instances of this concept might be an instance of this target concept, whereas others are not. Hence, there is a classification problem for instances of a concept mapped as a generalization of another concept.

- **Faulty mappings**, which are due to human errors in defining the mappings. Often this is caused by an expert not understanding the involved AK models correctly. The indirect mapping approach is more vulnerable to this problem than the direct mapping approach, as it uses two mappings instead of one.
Both garbage data and lost data are best illustrated using an indirect mapping approach, although they also occur in the direct mapping approach. Figure 2 presents an example of this. In the figure, the three circles represent three different AK models (i.e. S, T and central model C). Inside the circles reside $x_S$, $y_S$, $x_C$, $y_C$ and $x_T$, $y_T$, which are concepts from models S, C and T respectively. The mappings are indicated with arrows: the dotted arrow lines correspond to an indirect mapping, while the others to a direct mapping.

In the figure, lost data are created due to the inability to map concept $y_C$ to a concept of $T$. In this case, we know through the direct mapping that $y_C$ should have been mapped to concept $y_T$. However, we only know this holds for instances of $y_S$ and this might not be the case for $y_C$. Thus, the amount of relevant data of model $S$ that can be retrieved is reduced. Garbage data are created in this example by the "faulty" mapping from $x_C$ to $y_T$. Although this mapping makes perfect sense in the context of models C and T, we know from the direct mapping between models S and T that the instances of $x_S$ have nothing to do with the concept $y_T$. Hence, garbage data are created, which contaminates the relevant data in the query result.

![Figure 2](image_url)

Figure 2  Scenarios of lost data and garbage data with indirect mapping approach

### 3.4.4 Definition of AK sharing quality

The query-based scenario in section 3.4.1 is a typical activity in the field of IR. To define the quality of such queries, IR theory defines the concepts of **recall** and **precision**. These concepts could therefore also be used to quantify the AK sharing quality. The **recall** rate is the proportion of relevant data that is retrieved. The **precision** rate is the proportion of retrieved data that is relevant (Cleverdon, 1967). For the query-based scenario, the recall rate can be calculated by looking at the number of correctly classified instances to model $T$ compared to the total number of the instances in model $S$, i.e. \( \text{recall} = \frac{\text{correctly classified instances of } T}{\text{|S|}} \), in which the notation |Set| denotes the number of instances in a Set. The precision rate can be calculated by dividing the number of correctly classified instances to model $T$ to the total number of classified instances to model $T$, i.e. \( \text{precision} = \frac{\text{correctly mapped instances of } T}{\text{|T|}} \).

The goal of a good IR system (and therefore also the AK grid) is to retrieve as many relevant data as possible (i.e. have a high recall), and very few non-relevant data (i.e. have a high precision). Unfortunately, these two goals have proven to be quite contradictory. Techniques that tend to improve recall tend to hurt precision and vice versa.
3.4.5 Prediction of precision and recall

A problem in using the recall and precision rate as quantifications of the AK sharing quality is that it requires knowledge of the instances of the involved AK models. This is problematic, as capturing AK is the most expensive activity for sharing AK (see section 3.3). Instead, we would like to predict the recall and precision rate before AK is being captured. Hence, such a prediction may only use limited information, such as concepts and concept mappings.

As we want to compare a direct mapping approach with an indirect one as mentioned in section 3.2, we would like to use a relative precision and recall definition. We can assume that a direct mapping gives the best mapping result. Therefore, we normalize the precision and recall rate to the direct mapping. To do so, we redefine the concepts of relevant data, retrieved data, and relevant retrieved data introduced in IR theory, and represent them in terms of the query-based scenario. Table 1 presents an overview of these redefined terms.

Table 1 Redefined terms for relative precision and recall calculation of an indirect mapping approach

<table>
<thead>
<tr>
<th>Set</th>
<th>IR Theory</th>
<th>Query-based scenario</th>
<th>Set Symbol</th>
</tr>
</thead>
<tbody>
<tr>
<td>Relevant data</td>
<td>The data that the user is querying for</td>
<td>The instances classified from $S$ to $T$ with a direct mapping</td>
<td>$DM$</td>
</tr>
<tr>
<td>Retrieved data</td>
<td>The data retrieved by an IR system to the user query using different retrieval methods</td>
<td>The instances classified from $S$ to $T$ with an indirect mapping</td>
<td>$IM$</td>
</tr>
<tr>
<td>Relevant retrieved data</td>
<td>The subset of the retrieved data that match with the user query</td>
<td>The instances that have been classified both by the direct and indirect mapping approaches</td>
<td>$DM \cap IM$</td>
</tr>
</tbody>
</table>

Using the definitions in Table 1, the relative precision $P$ and recall $R$ can be calculated as follows:

$$P = \frac{|DM \cap IM|}{|IM|} \quad \text{and} \quad R = \frac{|DM \cap IM|}{|DM|}$$

When predicting the relative precision and recall, the problem is how many instances these three sets (i.e. $DM$, $IM$ and $DM \cap IM$) contain. We introduce the concept of set distribution $D$ to address this problem. A set distribution is defined as the fraction of the number of instances a set contains to the number of instances of a fixed superset $|S|$ ($S$ is the source model in the query-based scenario). Let $D_{Set}$ be the set distribution of the Set. We do not know the exact value of set distribution defined in Table 1, as we do not have the instances. Therefore, we predict the set distribution. Let $D'_{Set}$ be the prediction of a set distribution $D_{Set}$, then the prediction of precision $P'$ and recall $R'$ can be calculated as follows based on formula 1:

$$D_{Set} = \frac{|Set|}{|S|}, \quad D'_{Set} = \frac{|Set'|}{|S'|}, \quad P' = \frac{D'_{DM \cap IM}}{D'_{IM}} \quad \text{and} \quad R' = \frac{D'_{DM \cap IM}}{D'_{DM}}$$

4 Cost prediction

The cost of AK sharing is composed of five aspects: modeling, capturing, mapping, evolution, and extension costs (see section 3.3). Predicting the costs is relatively easy compared with quality prediction. To quantify these costs, we use the parameters defined as follows:

- $n$, the number of AK models involved with AK sharing in the knowledge grid.
- $m$, the average number of concepts per AK model.
- $k$, the average number of instances per AK model.
- $c$, the number of concepts in the central model for the indirect mapping approach. Note that $c \approx m$, as the central model will be similar in complexity to most AK models.
Using these parameters, we can predict the order of magnitude of the cost for AK sharing for the five different aspects:

- **Modeling costs.** The modeling costs will predominantly dependent on the number of models \((n)\) and the number of concepts these models have \((m)\). In addition, the familiarity with the domain being modeled has also an influence. Assuming this is constant for domain experts, modeling costs are \(O(m \times n)\) for the direct mapping approach. For the indirect mapping approach, also the central model needs modeling. Consequently, the costs become \(O(m \times n + c) \approx O(m \times n + m) = O(m \times (n + 1)) = O(m \times n)\). Thus, there is no significant difference in modeling costs between both mapping approaches.

- **Capturing costs.** The capturing costs are the most dominant costs for sharing AK using model mappings, as the number of instances is typically much bigger than the number of models and concepts involved, i.e. \(k \gg m, n\). The order of magnitude of the capturing costs are directly related to the number of instances, which is the number of models times the average number of instances per model, i.e. \(O(n \times k)\). This holds for both mapping approaches.

- **Mapping costs.** The effort required for the mappings depends on the amount of concept mappings that should be considered. For the direct mapping approach, this is \(O(n \times m \times (n - 1)) = O(n^2 \times m)\), as every concept of every model should be considered whether it maps to another concept of all other models. In the indirect mapping approach, every concept is mapped onto the central model and vice versa. No other models have to be considered in this mapping. The costs of this mapping is therefore \(O(n \times (m + c)) \approx O(n \times m)\).

- **Evolution/Extension costs.** The evolution costs can be quantified considering a scenario in which one AK model is changed. The extension costs can be quantified in a scenario of extending the AK grid with a new AK model. In both the direct and the indirect approach, all the instances and mappings of the new or updated model need to be created or verified. The costs at the instance level have the same order of magnitude in both approaches, as the cost of the individual operation doesn’t matter, only the number of operations counts. If this is the case, all the instances need to be verified and the created mapping to and from the model should be reconsidered. Thus the evolution costs depend on the mapping approach taken. For the direct mapping, the evolution costs is \(O(k + 2 \times (n - 1) \times m) = O(k \times n)\). Since every model in the grid maps directly back to the changed model, all these mappings need to be verified. For the indirect mapping approach, only the mappings to and from the central model need to be examined. The costs for an indirect mapping approach is \(O(k + m \times 2) = O(k + m)\), assuming that the central model does not have to change. This is reasonable, as the other models already had a reasonable mapping to the central model. However, if the central model needs to be changed, the cost can be up to a maximum of \(O(k + c \times n + m \times n) \approx O(k + 2 \times (m \times n)) = O(k + m \times n)\), which is equal to the costs of a direct mapping approach.

5 Instance mapping quality prediction

In this section, a closer look is taken at how the quality of AK sharing could be predicted. In section 5.1, three different approaches are presented for this purpose. For one of these approaches, sections 5.2 and 5.3 present the calculation methods and formulas.

### 5.1 Mapping Quality Prediction Models

In section 3.4.5, it was argued that the quality of AK sharing should be assessed by the precision and recall rate using predictions of set distributions (see formula 2). The value of these set distributions (i.e. \(D_{DM}, D_{IM}, \) and \(D'_{DM,IM}\)) depends on the instance classification results. This in turn is based on the concept mapping relationships between AK models. Consequently, the prediction of set distribution can be calculated using the set distribution prediction of all individual concept mapping relationships.
The individual concept mapping relationships are influenced by several aspects. To make fair predictions about them and their associated set distributions, a prediction model should either take them into account or make assumptions about them. In short, these aspects are the following:

- The relative importance of a concept in an AK model. For certain use-cases, some concepts are more important than others. Thus these concepts have a bigger impact on the perceived AK sharing quality.
- The instance distribution of each concept in the AK model, i.e. some concepts have many more instances than other concepts. Hence, good mappings for the instances of these concepts greatly influences the overall sharing quality.
- The type of instance classification employed: manual or automated classification. In principle, a manual classification can always make correct classifications. For an automated classification, i.e. a classification tool, the result doesn’t have to be correct for every instance mapping. Consequently, instances are incorrectly classified and/or are lost during the mapping process.
- The quality of the automatic classification. If an automatic instance classification tool is employed, the quality of this tool directly affects the AK sharing quality: the better the tool is, more instances will be mapped and classified correctly.

The more of these aspects we take into account, the better the prediction model we can come up with. However, this comes at the cost of additional complexity. To deal with these aspects, we have defined three different prediction models each with their own set of assumptions. In order of complexity, these models are the following:

**Simple MQPM (SMQPM)**
- All concepts are equally important;
- All instances in a AK repository are evenly distributed over the AK concepts;
- We use a perfect instance classification tool for the instance classification by which all instances will be smartly classified into correct concepts;

**Random instance classification MQPM (RMQPM)**
- All concepts are equally important;
- All instances in a AK repository are evenly distributed over the AK concepts;
- We use a random instance classification tool for the instance classification by which all instances will be classified into possible concepts randomly;

**Advanced MQPM (AMQPM)**
- Not all concepts are equally important;
- The domain expert predicts a more realistic instance distribution in a AK repository over the AK concepts;
- We use a random instance classification tool for the instance classification by which all instances will be classified into possible concepts randomly;

Of these three prediction models, the SMQPM has the most optimistic assumptions in which the instance classification tool classify perfectly the instances into correct concepts. In this case the prediction of a theoretical maximum precision \( \hat{P}_{SMQPM} \) and recall \( \hat{R}_{SMQPM} \) can be achieved. The RMQPM has the most pessimistic assumptions in which the instance classification tool classifies the instances into possible concepts randomly. In that case the prediction of a theoretical minimum precision \( \hat{P}_{RMQPM} \) and recall \( \hat{R}_{RMQPM} \) can be achieved. The AMQPM has the most realistic assumptions compared with those in SMQPM and RMQPM. In that case the prediction of precision \( \hat{P}_{AMQPM} \) and recall \( \hat{R}_{AMQPM} \) is theoretically closer to the real case, and \( \hat{P}_{RMQPM} \leq \hat{P}_{AMQPM} \leq \hat{P}_{SMQPM} \), \( \hat{R}_{RMQPM} \leq \hat{R}_{AMQPM} \leq \hat{R}_{SMQPM} \).

In this paper, the focus is on the SMQPM. The other two prediction models, i.e. RMQPM and AMQPM, will be investigated in the future.
5.2 SMQPM calculation rules

The calculation rules for SMQPM are based on the aforementioned assumptions and the effect these assumptions have on the set distributions. To be more precise, the predicted set distributions \(D'_{DM}, D'_{IM}\) and \(D'_{DM\cap IM}\) are calculated using the set distribution prediction of all the individual concept mapping relationships. To be concise and to differentiate from the set distribution concept defined in section 3.4.5, the set distribution of individual concept mapping relationships is named the concept mapping set distribution. The calculation rules for the prediction of this concept mapping set distribution is based on different concept mapping relationships. The following symbols are used to describe the effect of these mapping relationships:

- \(x_S\) and \(x_T\) are concepts from two AK models \(S\) and \(T\). A concept mapping relationship from \(x_S\) to \(x_T\) is normalized as a triple \(<x_S, m, x_T>\), in which \(m\) is the mapping relationship from \(x_S\) to \(x_T\). The concept mapping relationships include equivalentClass, subClassOf, superClassOf (inverseOf subClassOf), disjointWith and noMatchingPair, which can be readily represented in RDF Schema (Brickley & Guha, 2004) or OWL (Dean et al., 2004).
- To keep things simple, other mapping relationships like partOf, compositionOf are not considered in this model.
- \(Noc(x)\) denotes the Number of Concepts of \(x\). For the triple \(<x_S, m, x_T>\),
  - if \(m \neq \text{noMatchingPair}\), then \(Noc(x_S) = 1\) and \(Noc(x_T) \geq 1\), which means that the concept mapping relationship maps a concept 1 to 1 or 1 to many;
  - if \(m = \text{noMatchingPair}\), then \(Noc(x_S) = 1\) and \(Noc(x_T) = 0\), which means that there is no mappable concept for \(x_S\);
- \(D'( <x_S, m, x_T> )\) denotes the prediction of the concept mapping set distribution of an individual concept mapping relationship represented by the triple \(<x_S, m, x_T>\). Its real value, \(D( <x_S, m, x_T> )\), is the fraction of the number of instances classified from concept \(x_S\) to \(x_T\) to the number of instances of \(x_S\), i.e. \(D( <x_S, m, x_T> ) = \frac{|x_S \rightarrow x_T|}{|x_S|}\). Figure 3 illustrates this with \(x_S\), \(x_T\), and \(x_S \rightarrow x_T\) being sets of instances. With the assumption of an even distribution of instances over the concepts in SMQPM, we can assign a constant \(C\) as number of instances of all concepts, i.e. \(|x_S| = C\). Thus for the prediction of \(D'( <x_S, m, x_T> )\), we get:
  - \(0 \leq D'( <x_S, m, x_T> ) \leq 1\);
  - \(D'( <x_S, m, x_T> ) = 0\), if \(m = \text{noMatchingPair}\);
  - \(D'( <x_S, m, x_T> ) = 1\), if \(m \neq \text{noMatchingPair}\) and all the instances of concept \(x_S\) can be classified as the instances of concepts \(x_T\);

![Diagram](image.png)  
**Figure 3** A concept mapping set distribution based on a concept mapping relationship from \(x_S\) to \(x_T\)
In the remainder of this section, the calculation rules are presented to predict the **concept mapping set distribution** (i.e. \(D'(x_S, m, x_T)\)) and the **side-effect concept mapping set distribution**. The latter distribution describes how the mapping indirectly affects the instance distribution of other concepts. For each different type of concept mapping relationship, i.e. equivalentClass, subClassOf, superClassOf, noMatchingPair, different calculation rules exist. We explain which rules should be used in which situation.

### 5.2.1 equivalentClass

**Rule 1. equivalentClass concept mapping relationship**

**Figure 4** equivalentClass concept mapping relationship from \(x_S\) to \(x_T\)

- **Concept mapping set distribution**
  - **Calculation**: \(D'(x_S, m, x_T) = 1\) (\(m = \text{equivalentClass}\))
  - **Reason**: Since \(x_S\) is equivalentClass of \(x_T\), any instance of \(x_S\) is also the instance of \(x_T\), i.e. \(|x_S \rightarrow x_T| = |x_S| = C\), then \(D'(x_S, m, x_T) = \frac{|x_S \rightarrow x_T|}{|x_S|} = 1\).

- **Side-effect concept mapping set distribution**
  - **Condition**: \(y_T\) is a concept in model \(T\) and is a direct subClassOf \(x_T\). All the concepts \(y_T\) are disjointWith each other.
  - **Calculation**: \(D'(x_S, m, y_T) = \frac{1}{NcC(y_T) + 1}\) (\(m = \text{Rule 1}\)), in which \(NcC(y_T)\) denotes the number of concepts as \(y_T\).
  - **Reason**: With the assumption of even distribution of instances in SMQPM, all the instances of \(x_T\) will be distributed evenly in its direct subclasses (as \(y_T\)) plus one dummy subclass, which represents the concept of instances not covered by all the explicit direct subclasses of \(x_T\). An example of this is presented in Figure 5. All the concepts \(y_T\) are disjointWith each other, so there are no instances in the intersection of different \(y_T\). With \(|x_S \rightarrow x_T| = |x_S| = C\), \(|x_S \rightarrow y_T| = \frac{|x_S \rightarrow x_T|}{NcC(y_T) + 1} = \frac{C}{NcC(y_T) + 1}\), then \(D'(x_S, m, y_T) = \frac{|x_S \rightarrow y_T|}{|x_S|} = \frac{1}{NcC(y_T) + 1}\).

**Figure 5** Instances classification example of internal subClassOf relationship with one subclass \(y_T\)
5.2.2 `subClassOf`

**Rule 2. `subClassOf` with `disjointWith` concept mapping relationship**

![Diagram](image)

**Figure 6** `subClassOf` concept mapping relationship from $x_S$ to $x_T$ with $x_S$ disjointWith $y_T$

- **Concept mapping set distribution**
  - **Calculation**: $D'(\langle x_S, m, x_T >) = 1 \ (m = \text{`subClassOf'})$
  - **Reason**: Since $x_S$ is `subClassOf` $x_T$, any instance of $x_S$ is also an instance of $x_T$, i.e. $|x_S\rightarrow x_T| = |x_S| = C$, then $D'(\langle x_S, m, x_T >) = \frac{|x_S\rightarrow x_T|}{|x_S|} = 1$.

- **Side-effect concept mapping set distribution**
  - **Condition**: $y_T$ is a concept in model $T$, and is a direct `subClassOf` $x_T$, and $x_S$ is `disjointWith` $y_T$.
  - **Calculation**: $D'(\langle x_S, m, y_T >) = 0 \ (m = \text{Rule 2})$
  - **Reason**: Since $x_S$ is `disjointWith` $y_T$, there are no instances in the intersection between $x_S$ and $y_T$. With $|x_S\rightarrow y_T| = 0$, then $D'(\langle x_S, m, y_T >) = \frac{|x_S\rightarrow y_T|}{|x_S|} = 0$.

**Rule 3. `subClassOf` without `disjointWith` concept mapping relationship**

![Diagram](image)

**Figure 7** `subClassOf` concept mapping relationship from $x_S$ to $x_T$ without $x_S$ disjointWith $y_T$

- **Concept mapping set distribution**
  - **Calculation**: $D'(\langle x_S, m, x_T >) = 1 \ (m = \text{`subClassOf'})$
  - **Reason**: Here the same reason applies as for the concept mapping set distribution in Rule 2.

- **Side-effect concept mapping set distribution**
  - **Condition**: $y_T$ is a concept in model $T$ and is a direct `subClassOf` $x_T$. $x_S$ is not `disjointWith` $y_T$, which is the default situation as no mapping relationship is defined between them. All concepts $y_T$ are `disjointWith` each other.
  - **Calculation**: $D'(\langle x_S, m, y_T >) = \frac{1}{N_{oc(y_T)} + 1} \ (m = \text{Rule 3})$
  - **Reason**: The same reason applies as for the side-effect concept mapping set distribution of Rule 1.
5.2.3 superClassOf

Rule 4. superClassOf concept mapping relationship

\[ x_S(C) \xrightarrow{\text{superClassOf}} x_T \xrightarrow{} y_T \]

Figure 8 superClassOf concept mapping relationship from \( x_S \) to \( x_T \)

- Concept mapping set distribution
  - Calculation: \( D'(\langle x_S, m, x_T \rangle) = \frac{1}{\text{Not}(x_T)+1} \) (\( m \) =superClassOf)
  - Reason: Since \( x_S \) is superClassOf \( x_T \), then \( x_T \) is subClassOf \( x_S \). The same reason as that for side-effect concept mapping set distribution in Rule 1 applies.

- Side-effect concept mapping set distribution
  - Condition: \( y_T \) is a concept in model T, and is a direct subClassOf \( x_T \), and \( x_S \) is not disjointWith \( y_T \), which is a default situation between \( x_S \) and \( y_T \) if there is no mapping relationship defined between them. All concepts as \( x_T \) are disjointWith each other, and all concepts as \( y_T \) are also disjointWith each other.
  - Calculation: \( D'(\langle x_S, m, y_T \rangle) = \frac{1}{\text{Not}(y_T)+1} \times \frac{1}{\text{Not}(x_T)+1} \) (\( m \) =Rule 4)
  - Reason: The same reason as that for side-effect concept mapping set distribution of Rule 1. With \( |x_S| = C, |x_S\rightarrow x_T| = \frac{|x_S\rightarrow x_T|}{\text{Not}(x_T)+1}, |x_S\rightarrow y_T| = \frac{|x_S\rightarrow y_T|}{\text{Not}(y_T)+1} \), then \( D'(\langle x_S, m, y_T \rangle) = \frac{|x_S\rightarrow x_T|}{|x_S\rightarrow x_T|} = 1, D'(\langle x_S, m, y_T \rangle) = \frac{|x_S\rightarrow y_T|}{|x_S\rightarrow y_T|} = 1 \).

5.2.4 noMatchingPair

Rule 5. noMatchingPair concept mapping relationship

\[ x_S(C) \xrightarrow{\text{noMatchingPair}} \]

Figure 9 noMatchingPair concept mapping relationship from \( x_S \)

- Concept mapping set distribution
  - Calculation: \( D'(\langle x_S, m, x_T \rangle) = 0 \) (\( m \) =noMatchingPair)
  - Reason: Since \( x_S \) has noMatchingPair of \( x_T \), any instance of \( x_S \) is not the instance of \( x_T \), i.e. \( |x_S\rightarrow x_T| = 0 \), then \( D'(\langle x_S, m, x_T \rangle) = \frac{|x_S\rightarrow x_T|}{|x_T|} = 0 \).

5.3 Prediction of set distribution for precision and recall

In this section, the calculation formulas are presented for the prediction of the set distribution, i.e. \( D_{DM}', D_{IM}', \) and \( D_{DM\cap IM}' \). The calculation formulas make use of the earlier presented calculation rules of section 5.2.

5.3.1 \( D_{DM}' \) calculation

We use definition from section 3.4.5: \( D_{DM}' = \frac{|DM'|}{|S'|} \). With the assumption of even instance distribution over concepts in SMQPM, the prediction value of the set \( |S'| \) is the number of
concepts in AK model $S$ times the constant $C$ which is the number of instances of each concept. The set $|DM'|$ is calculated by the sum of the concept mapping set distributions and the side-effect concept mapping set distributions of all the concept mappings from model $S$ to $T$ multiplied by the constant $C$. The concept mapping relationship from one concept $x_S$ in model $S$ to concepts in model $T$ can be a 1 to 1 or 1 to multiple concepts mapping, so we use $x_T$ to represent the set of concepts mapped from $x_S$. Detailed calculation formulas are presented in formula 3. In this formula, $n$ is the number of mapping relationships (including direct mapping or side-effect mapping caused by calculation rules) from $x_S$ to $T$ and $NoC(S)$ is the number of concepts in AK model $S$:

$$D'(x_S, m, x_T) = \sum_{j=1}^{n} D'(x_S, m, x_T^j), (x_T = \{x_T^1, .., x_T^n\} \subset T);$$

$$D'_{DM} = \frac{|DM'|}{|S'|} = C \times \sum_{i=1}^{NoC(S)} D'(x_S^i, m, x_T^i) \times \frac{C \times NoC(S)}{\sum_{i=1}^{NoC(S)} D'(x_S^i, m, x_T^i)}$$

5.3.2 $D'_{IM}$ calculation

$D'_{IM}$ is the prediction of set distribution based on the concept mappings from $S$ to $T$ with the indirect mapping approach, in which concept mapping relationships from concepts of model $S$ to central model $C$, and from the mapped concepts in $C$ to $T$ will occur. $D'_{IM}$ can be calculated in a similar way as $D'_{DM}$. The only difference is that we use $D'_{C}(x_S, m, x_T)$ to represent a prediction of the set distribution of individual concept mapping relationships through model $C$ based on the two mapping relationships represented by triples $<x_S, m, x_C>$ and $<x_C, m, x_T>$. In these triples, $x_C$ represents the set of concepts of the central model $C$ mapped from $x_S$. $x_T$ represents the set of concepts mapped from $x_C$. To distinguish it from other kinds of concept mapping set distributions, $D'_{C}(x_S, m, x_T)$ will be called as the combined concept mapping set distribution. Its calculation formula is described in two steps. In the first step, the concept mapping set distribution for each $x_C^j$ (concept mapped from $x_S$ to central model $C$) is calculated by the sum of the product of the concept mapping set distribution and the side-effect concept mapping set distribution from $x_S$ to $x_C^j$ and $x_C^j$ to $T$. In the second step, the combined concept mapping set distribution for $x_S$ is calculated by the sum of the concept mapping set distribution for each $x_C^j$ mapped from $x_S$ to $C$. Detailed calculation formulas are presented in 4. In this formula, $n$ is the number of mapping relationships (including direct mapping or side-effect mapping caused by calculation rules) from $x_S$ to $C$. $l(j)$ is a function of parameter $j$ and calculates the number of mapping relationships, including direct mappings and side-effect mappings caused by the calculation rules, from $x_C^j$ to $T$:

$$D'_{C}(x_S, m, x_T) = \sum_{j=1}^{n} \sum_{k=1}^{l(j)} D'(x_S, m, x_C^j) \times D'(x_C^j, m, x_T^k),$$

$$x_T = \{(x_T^1, .., x_T^k) \cup \{x_T^1, .., x_T^{l(1)}\} \cup \{x_T^1, .., x_T^{l(j)}\} \cup \{x_T^1, .., x_T^{l(n)}\}\} \subset T;$$

$$D'_{IM} = \frac{|IM'|}{|S'|} = C \times \sum_{i=1}^{NoC(S)} D'_{C}(x_S^i, m, x_T^i) \times \frac{C \times NoC(S)}{\sum_{i=1}^{NoC(S)} D'_{C}(x_S^i, m, x_T^i)}$$

5.3.3 $D'_{D(M|I)M}$ calculation

$D'_{D(M|I)M}$ is the prediction of the set distribution of the instances that belong to both the $DM$ and $IM$ sets. It is calculated in a similar fashion as $D'_{IM}$. The only difference is that part of the combined concept mapping set distribution in $D'_{IM}$, whose combined concept mapping relationships (indirect mapping caused by two concept mappings) do not belong to the direct
concept mapping relationships from $S$ to $T$, should be taken out. The reason is that this part of the combined concept mapping set distribution is not relevant to the concept mapping set distribution in $D'_{DM}$. We use $D'_{RC}(<x,S,m,x_T>)$ to represent the relevant combined concept mapping set distribution in $D'_{IM}$. Its calculation is the same as that for $D'_C(<x,S,m,x_T>)$, except for an additional parameter $r$, $r = 1$ when the combined concept mapping set distribution is relevant and $r = 0$ when it is not. Detailed calculation formulas are given below (5), in which all the parameters except for $r$ have the same meaning as those in section 5.3.2:

$$D'_{RC}(<x,S,m,x_T>) = \sum_{j=1}^{n} \left( \sum_{k=1}^{l(j)} D'(<x,S,m,x_{C^j}>) \times D'(<x_{C^j},m,x_{T^k}>) \times r \right),$$

$$(x_C = \{x_{C^1}, x_{C^2}, ..., x_{C^n}\} \subset C, x_T = \{x_T^1, x_T^2, ..., x_T^{l(1)}\} \cup \{x_T^1, x_T^2, ..., x_T^{l(j)}\} \cup \{x_T^1, x_T^2, ..., x_T^{l(n)}\} \subset T);$$

$$D'_{DM\cap IM} = \frac{|DM \cap IM'|}{|S'|} = \frac{\sum_{i=1}^{NoC(S)} D'_{RC}(<x_S^i,m,x_T^i>)}{NoC(S)}$$

### 5.4 Example of instance classification quality prediction

In this section, we exemplify the instance classification prediction. In this example, the LOFAR AK model (Jansen et al., 2008) is used as the source model $S$ and Kruchten’s ontology (Kruchten, 2004) as the target model $T$. The core model proposed by de Boer et al. (2007) acts as the central model $C$. The LOFAR AK model is used to document the AK in the LOFAR project; this knowledge needs to be shared and reused over more than 25 years. Kruchten’s ontology is an ontology of architectural design decisions which comprise a major part of AK as defined in (Kruchten et al., 2005). The core model is a first attempt to cover all the concepts from different AK models and is thus a good candidate for a central model. Due to space limitations, the detailed concept mapping relationships and calculation of set distribution (i.e. $D'_{DM}$, $D'_{IM}$ and $D'_{DM\cap IM}$) of this example can be found in (Liang, et al., 2008). Note, that the calculation result of $D'(<x,S,m,x_T>) > 1$ is regarded as $D'(<x,S,m,x_T>) = 1$ for the sum calculation in formulas 3,4 and 5. Since $D'(<x,S,m,x_T>) \in [0,1]$, as defined in section 5.2. We simply present the calculation results as follows: with $D'_{DM} = 0.835$, $D'_{IM} = 0.835$ and $D'_{DM\cap IM} = 0.680$, then

$$P' = \frac{D'_{DM\cap IM}}{D'_{IM}} = \frac{0.680}{0.835} = 0.814 \text{ and } R' = \frac{D'_{DM\cap IM}}{D'_{DM}} = \frac{0.680}{0.835} = 0.814$$

### 6 Instance mapping experiment

In this section, a mapping experiment at the instance level for AK sharing is presented to validate the SMQPM. The experiment process is divided into two steps as illustrated in Figure 10 and Figure 11. We use the same AK models, i.e. $S$, $T$ and $C$, as defined in section 5.4 for the instance mapping quality prediction. Note, that the "instance mapping" in this section is performed manually by domain experts, while the "instance classification" in the previous sections is performed automatically by an instance classification tool. The sample input for this experiment is a software architecture document (33 pages) of the LOFAR software system for data processing, denoted as LOFAR.DOC.

The first step is the instance mapping using a direct mapping approach. In this step, we manually annotate the LOFAR.DOC using the LOFAR AK model and Kruchten’s ontology to construct two AK repositories. Both originate from the same architecture document (LOFAR.DOC), but use different AK models. After this, we map the AK instances from the LOFAR AK repository to the Kruchten AK repository based on the direct mapping relationship from the LOFAR AK model to Kruchten’s ontology. In the instance mappings, only one mapping relationship is defined
between instances: `sameAs`. For example, the text "In the data factory architectural view the focus is on the configuration" (instanceA) is an instance of concept `Concern` in the LOFAR AK repository, while it is an instance of the concept `Requirement` of the Kruchten AK repository. With the direct mapping relationship: `Concern` is `superClassOf` `Requirement` and by the domain expert analysis: instanceA is an instance of concept `Requirement` we create the instance mapping: `instanceA(type:Concern)` `sameAs` `instanceA(type:Requirement)`. The result of the first step is the set of instances mapped from the LOFAR to the Kruchten AK repository, i.e. the set `DM`. With the set of instances in the source LOFAR AK repository, we can calculate the set distribution of set `DM` using: 

\[ D_{DM} = \frac{|DM|}{|LOFAR|} \]

The second step is the instance mapping using the indirect mapping approach. In this step, we manually annotate the LOFAR.DOC using the core model. The two AK repositories constructed in the previous step are reused to construct a total of three AK repositories that originate from the same architecture document (LOFAR.DOC), but use different AK models. Next, we map the AK instances from the LOFAR AK repository to the core model AK repository and subsequently to the Kruchten AK repository using the direct mapping relationships for both instance mappings as presented in Figure 11. In both mappings, the instance mapping relationship `sameAs` is used similar to the first step. The result of the second step is the set of instances mapped from the LOFAR to the Kruchten AK repository through the core model, i.e. the set `IM`. With the set of instances in the source LOFAR AK repository, we can calculate the set distribution of set `IM`: 

\[ D_{IM} = \frac{|IM|}{|LOFAR|} \]

Finally, we compare the instance mappings between the two sets `DM` and `IM` to determine which instance mapping are relevant and which are not in the set `IM`, then we can get the
intersection of sets $DM \cap IM$. Then we can calculate the set distribution of set $DM \cap IM$: $D_{DM \cap IM} = \frac{|DM \cap IM|}{\text{LOF AR}}$. With the value of set distribution ($D'_{DM}$, $D'_{IM}$, and $D'_{DM \cap IM}$) and calculation formula 2 defined in section 3.4.5, we can get the precision ($P$) and recall ($R$) for this instance mapping experiment: $P = 0.958$ and $R = 0.912$.

7 Comparison analysis

In this section, we compare the direct and indirect mapping approaches with respect to their quality and cost. In addition, the prediction of the sharing quality is compared with the real value. An overview of the results is presented in Table 2. For both the precision and the recall, normalized numbers are shown to ease the comparison between the two mapping approaches. The values of the direct mapping ($P' = R' = P = R = 1$) form the basis for this normalization. The prediction and real value of the precision and recall of the indirect mapping approach come from the values ($P'$, $R'$, $P$ and $R$) calculated in section 5.4 and 6. The cost of AK sharing consists of five aspects: modeling (MOD), capturing (CAP), mapping (MAP), evolution (EVO), and extension (EXT) costs, as presented in section 4.

Table 2 Comparison of the direct and indirect mapping approach

<table>
<thead>
<tr>
<th>AK Sharing Approach</th>
<th>Prediction or Real</th>
<th>Quality</th>
<th>Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>Direct Mapping</td>
<td>Prediction</td>
<td>$O(m \times n)$</td>
<td>$O(n^2 \times m)$</td>
</tr>
<tr>
<td></td>
<td>Real</td>
<td>34</td>
<td>34</td>
</tr>
<tr>
<td>Indirect Mapping</td>
<td>Prediction</td>
<td>$O(m \times n)$</td>
<td>$O(n \times k)$</td>
</tr>
<tr>
<td></td>
<td>Real</td>
<td>0.958</td>
<td>58</td>
</tr>
</tbody>
</table>

Looking at the table, we can conclude that for the sharing quality our estimation was too pessimistic. This is reasonable, as the LOFAR AK model, the core model and Kruchten’s ontology all place stress on architectural design decisions, and therefore have many overlapping concepts in AK documentation. Comparing the direct and indirect mapping approaches with each other, we find, quite surprising, that for both the precision and recall we only lose 5% and 10% in quality when using an indirect mapping approach. This is partially due to the fact that the employed central model (the core model) has been influenced by the existence of the LOFAR AK model, thereby covering many of LOFAR model concepts to some extent. If we look at the cost, then an indirect mapping approach starts paying off when more AK models are involved in the knowledge grid. In that case, the mapping, evolution, and extension costs become considerably lower, as compared to the costs of a direct mapping approach.

Concluding, it seems that the indirect mapping approach loses some quality, although not much. The cost benefit is however huge, if more than three AK models are being used. However, these are very preliminary results, as only two AK models, one central, and one architectural document have been tested so far. Further experimentation on several AK models and architecture documents is needed to draw more firm general conclusions.

8 Conclusions and future work

In this paper, we presented a mapping quality prediction model (SMQPM) that is composed of the following: (1) It makes specific assumptions for the quality prediction of AK sharing. (2) It defines evaluation criteria for AK sharing quality by introducing the precision and recall from the IR theory. (3) It specifies a calculation method and rules for the prediction of these criteria. The direct and indirect mapping approaches are evaluated in terms of the quality and cost for AK sharing. According to the comparison analysis result, stakeholders involved with AK sharing can select an appropriate approach by trading off quality and cost in their own context. In order
to do so, one needs to consider the number of AK repositories involved with AK sharing, and the number of instances in those AK repositories.

We outline our future work in several points: (1) More AK models should be covered and AK repositories should be included for the validation of mapping quality prediction models. (2) The mapping quality prediction models RMQPM and AMQPM, that contain more realistic assumptions as specified in section 5.1 should be investigated. (3) The relationships between AK instances as specified in (Kruchten, 2004; de Boer et al., 2007) are lost in the currently proposed AK sharing scenarios, which result in traceability problems. For example, a relationship exists between the AK instances of concept Alternative and concept Decision Topic in that instanceA(type:Alternative) isProposedFor instanceB(type:Decision Topic) in an architecture design. A solution that retains the relationships between AK instances for AK sharing needs to be investigated. (4) Tool support for AK model mapping and the quality and cost prediction calculation needs to be implemented in order to automate the central model evaluation.

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